

Surname	Centre Number	Candidate Number
First name(s)		2



GCE AS/A LEVEL

2305U30-1



S25-2305U30-1

TUESDAY, 20 MAY 2025 – AFTERNOON

FURTHER MATHEMATICS – AS unit 3
FURTHER MECHANICS A

1 hour 30 minutes

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a Formula Booklet;
- a calculator.

INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** questions.

Take g as 9.8 ms^{-2} .

Write your answers in the spaces provided in this booklet. If you run out of space, use the additional page(s) at the back of the booklet, taking care to number the question(s) correctly.

INFORMATION FOR CANDIDATES

The maximum mark for this paper is 70.

The number of marks is given in brackets at the end of each question or part-question.

Sufficient working must be shown to demonstrate the **mathematical** method employed.

Answers without working may not gain full credit.

Unless the degree of accuracy is stated in the question, answers should be rounded appropriately.

You are reminded of the necessity for good English and orderly presentation in your answers.

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1	6	
2	13	
3	11	
4	7	
5	9	
6	10	
7	14	
Total	70	



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(b) Determine the value of $F.v$ when $t = 2$, clearly stating the units of your answer.

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- (b) Given that $m = 5$, calculate the magnitude and direction of the impulse exerted by A on B .

[3]



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3. At time $t = 0$, a drone A has position vector $(3\mathbf{i} - 10\mathbf{j} + 20\mathbf{k})\text{m}$ and is flying with constant velocity $(-\mathbf{i} + 2\mathbf{j} + \mathbf{k})\text{ms}^{-1}$. At time $t = 0$, another drone B has position vector $(-2\mathbf{i} + 30\mathbf{j} + 15\mathbf{k})\text{m}$ and is flying with constant velocity $(3\mathbf{i} - 4\mathbf{j} + 2\mathbf{k})\text{ms}^{-1}$.

(a) Write down the position vectors of A and B at time t seconds.

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(b) Given that AB is the distance between A and B at time t seconds, show that

$$AB^2 = 53t^2 - 530t + 1650.$$

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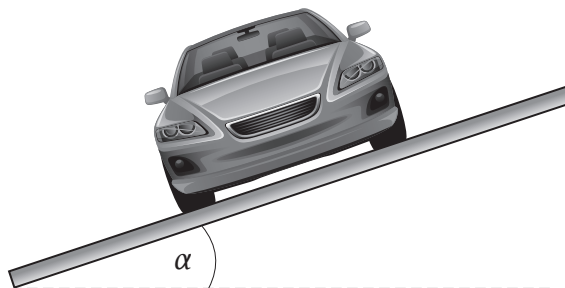


- (c) Determine the value of t when A and B are closest together. Hence find the least distance between A and B .

[4]



4. The diagram below shows a car, of mass 1500 kg, on a track banked at an angle α to the horizontal.



The car is moving in a horizontal circle of radius 150 m.

When the car is moving with a constant speed of $v \text{ ms}^{-1}$, it has no tendency to sideslip. The normal reaction of the track on the car is 17 150 N.

- (a) Show that α is approximately 31° .

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[4]



5. A light elastic string, of natural length 1.4 m and modulus of elasticity 156.8 N , has one end attached to a fixed point O and the other end attached to a particle P of mass $m\text{ kg}$.

Initially, P is held at rest at the point O . It is then released and allowed to fall under gravity.

- (a) Determine the extension in the string at the instant when the tension in the string is 36 N .

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- (b) Given that the kinetic energy of P is 15.12 J when it is 2 m below O , show that $m = 1.8$.

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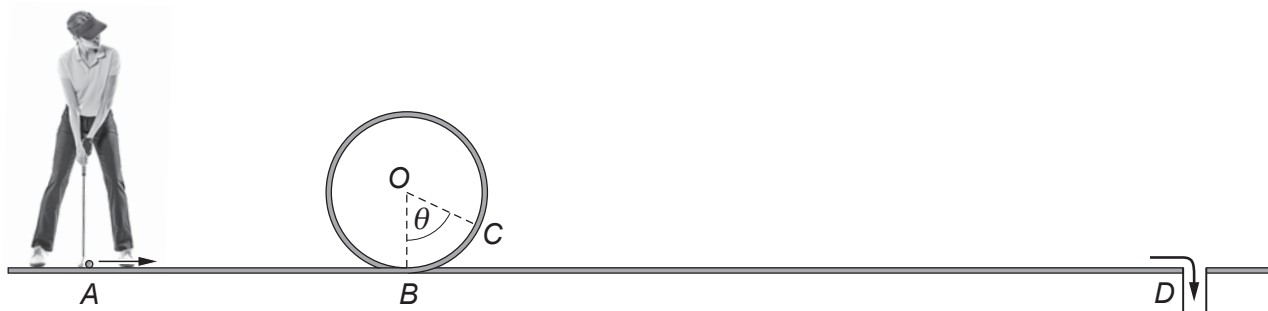
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7. The diagram below shows part of a 'Crazy Golf' course. This part of the course consists of a straight horizontal section AB , leading into a circular loop, followed by another straight horizontal section BD .

The objective of the game is to hit a golf ball, from rest at the point A , so that it remains in contact with the surface for its entire journey until it reaches the point D , where it is required to drop into a hole.



The loop section may be modelled as a vertical circle of radius 0.5 m and the ball as a particle of mass 0.04 kg . You may assume that the entire surface of the course is smooth and is set in the same vertical plane.

The ball is hit horizontally from A . At the point B , which is the lowest point of the circle, the speed of the ball is $u\text{ ms}^{-1}$.

- (a) When the ball is at a point C on the inside of the circular loop, the line OC makes an angle θ with the downward vertical.

- (i) Find, in terms of θ and u^2 , an expression for v^2 , where $v\text{ ms}^{-1}$ is the speed of the ball at C . [4]

- (ii) Show that the reaction of the surface on the ball at C , RN , is given by

$$R = 0.08u^2 - 0.784 + 1.176 \cos \theta. \quad [4]$$

- (iii) Given that the ball does not complete a full circle, but instead, it leaves the loop at a point where $\theta = 120^\circ$, calculate the value of u . [2]

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